

## Application of the isotope pairing technique in sediments where anammox and denitrification coexist

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### Web Appendix 1

#### Relationship between $N_2$ gasses produced via denitrification or anammox

**Denitrification**—In a  $^{15}N$  labeling experiment, the denitrification process will produce 3 isotopic  $N_2$  species,  $^{14}N^{14}N$ ,  $^{14}N^{15}N$ , and  $^{15}N^{15}N$ . If the ratio between  $^{15}N$  labeled and unlabeled  $NO_x^-$  species is constant in the  $NO_x^-$  reduction zone, the produced isotopic  $N_2$  species will be binomially distributed.

The ratio between  $^{14}N^{14}N$  and  $^{14}N^{15}N$  produced via denitrification, i.e.,  $D_{28}$  and  $D_{29}$ , respectively, will then be as follows:

$$\frac{D_{28}}{D_{29}} = \frac{x^2}{2 \cdot x \cdot y} = \frac{x}{2 \cdot y} = \frac{r_{14}}{2} \quad (1.1)$$

where  $x$  and  $y$  are the mole fractions of  $^{14}NO_x^-$  and  $^{15}NO_x^-$ , respectively, in the  $NO_x^-$  reduction zone—e.g.,  $x = \frac{^{14}NO_x^-}{[^{14}NO_x^- + ^{15}NO_x^-]}$ , and  $r_{14}$  is the ratio between  $^{14}NO_x^-$  and  $^{15}NO_x^-$  in the  $NO_x^-$  reduction zone.

$D_{28}$  can then be expressed as a function of  $D_{29}$ :

$$D_{28} = D_{29} \cdot \frac{r_{14}}{2} \quad (1.2)$$

Given binomial distribution of the produced  $N_2$  species the ratio between  $^{14}N^{15}N$  and  $^{15}N^{15}N$  produced via denitrification, i.e.,  $D_{29}$  and  $D_{30}$ , will be as follows:

$$\frac{D_{29}}{D_{30}} = \frac{2 \cdot x \cdot y}{y^2} = 2 \cdot r_{14} \quad (1.3)$$

$D_{29}$  and  $D_{30}$  can then be expressed as functions of each other:

$$D_{29} = 2 \cdot D_{30} \cdot r_{14} \quad (1.4)$$

$$D_{30} = \frac{D_{29}}{2 \cdot r_{14}} \quad (1.5)$$

From these equations it is possible to derive the equation used in the classical IPT. The classical IPT presumes that gen-

uine  $N_2$  production ( $p_{14}$ ) is equivalent to:

$$p_{14} = 2 \cdot D_{28} + D_{29} \quad (1.6)$$

By substitution with Eq. 1.4 and 1.5, this equation can be expressed as follows:

$$\begin{aligned} p_{14} &= r_{14} \cdot D_{29} + 2 \cdot D_{30} \cdot r_{14} \\ &= r_{14} \cdot (D_{29} + 2 \cdot D_{30}) \end{aligned} \quad (1.7)$$

According to Eq. 1.3,  $r_{14}$  can be expressed as:

$$r_{14} = \frac{D_{29}}{2 \cdot D_{30}} \quad (1.8)$$

and substituting  $r_{14}$  into Eq. 1.7 with this term gives:

$$p_{14} = \frac{D_{29}}{2 \cdot D_{30}} (D_{29} + 2 \cdot D_{30}) \quad (1.9)$$

which is the classical IPT term.

**Anammox**—In a  $^{15}N$ -labeling experiment the anammox process will produce 2 isotopic  $N_2$  species:  $^{14}N^{14}N$  and  $^{14}N^{15}N$ . If the ratio between  $^{15}N$  labeled and unlabeled  $NO_2^-$  species is constant in the  $NO_2^-$  reduction zone the ratio between  $^{14}N^{14}N$  and  $^{14}N^{15}N$  produced via anammox, i.e.,  $A_{28}$  and  $A_{29}$  can be estimated from simple probability mathematics.

$$\frac{A_{28}}{A_{29}} = \frac{x}{y} = r_{14} \quad (2.1)$$

Thus,  $A_{28}$  can be expressed as a function of  $A_{29}$ :

$$A_{28} = r_{14} \cdot A_{29} \quad (2.2)$$

Here we assume for the sake of simplicity that  $p$ ,  $q$  and  $r_{14}$  are all equivalent to the terms used above (see assumption 2 in the *Materials and procedures* section).